

Project Management Institute College of Performance Management



Statistical Methods Applied to Project Management



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• • Abstract





 An objective of project management is to have the capability to reliably predict cost and schedule outcomes

 The application of statistical methods to the cost and schedule indicators from EVM and ES is a well-founded means for providing the project management objective



Forecasting with EVM & ES
Discussion of Statistical Method
Application to Real Data
Analysis & Results



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- Summary
- Final Remarks

Forecasting with EVM & ES

• IEAC = BAC / CPI

- *IEAC* = *Independent Estimate at Completion*
- BAC = Budget at Completion
- CPI = Cost Performance Index = EV / AC

• IEAC(t) = PD / SPI(t)

- *IEAC(t) = IEAC(time)*
- PD = Planned Duration
- SPI(t) = Schedule Performance Index (time) = ES / AT





Forecasting Background

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 IEAC & CPI studies by Dr. Christensen et al (1990 – 2004)

- IEAC = BAC / CPI is Low Bound
- $|CPI(final) CPI(20\%)| \le 0.10$
- US DOD Acquisition Data
- IEAC(t) & SPI(t) studies by K. Henderson, Dr. Vanhoucke & S. Vandevoorde (2003 –)
 - Henderson & Vandevoorde validated ES concept with real data
 - Using simulation Vanhoucke & Vandevoorde showed ES to be a better schedule predictor than other EVMbased methods

• • Forecasting Dilemma

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- Without broad-based data from a variety of EVM & ES applications empirical study is incomplete
- Simulations may not be representative



 Statistical methods are long standing calculation techniques for inferring outcomes

Statistical Method

• Confidence Limits: the range of possible values which encompass the true value of the mean, at a specified level of confidence



• Mathematically

CL = Mean $\pm Z * \sigma/\sqrt{n}$

Mean – estimate of average from the sample

Z = value related to prescribed area within the Normal distribution

[generally 90% or 95% level of confidence]

 σ = estimate of the Standard Deviation

n = number of observations in the sample









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Complexity Elements

Normality of Data

- CPI & SPI(t) distributions appear lognormal
- Mean is logarithm of cumulative value of index
- $\sigma = \sqrt{(\Sigma(\ln \text{ period index}(i) \ln \text{ cum index})^2 / (n 1))}$

• Finite Population

- $AF_C = \sqrt{(BAC EV) / (BAC (EV/n))}$
- $AF_s = \sqrt{(PD ES) / (PD (ES/n))}$

• Fewer than 30 Observations

• Use Student-t Distribution



Use of Confidence Limits

 Intent is to show that Confidence Limits are reliable forecasts of bounds for cost and schedule outcomes

• $CL_{(\pm)} = In index(cum) \pm Z * (\sigma/\sqrt{n}) * AF$



• Forecast at Completion

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$$IEAC_{(low or high)} = BAC / EXP(CL_{(\pm)})$$

• $IEAC(t)_{(low or high)} = PD / EXP(CL(t)_{(\pm)})$

Study Method

 IEACs are iteratively computed for each newly added observation





 Upper and Lower Confidence Limits are tested using the statistical hypothesis test, <u>Sign Test</u>, at 0.05 significance

- Final Cost < IEAC_H
- Final Cost > IEAC_L
- Final Duration < IEAC(t)_H
- Final Duration > IEAC(t)_L

Study Method

• Desired test result is the alternative hypothesis, Ha (shown on previous chart)





- Test results are tabulated as Ha when value of test statistic is in the critical region (0.05) – and Ho when it is not
- From the Ha results for the projects, the probability of obtaining reliable results is computed



- Testing is conducted for various confidence levels and data sets
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- Confidence Levels: 90%, 95%, 98%
- Data Set: 10-100%, 30-100%, 60-100%
- Expectation: as Conf Level & Data% increase, reliability of forecast increases
- By combining confidence levels and data sets a generally reliable project cost and duration forecasting is sought

Real Data - Characterized







- 497 months of EVM data
- No re-plans
- Data from single MIS under one manager
- Cost range: \$291K \$6.08M
- Duration range: 17 50 months
- CPIcum range: 0.481 1.051
- SPI(t)cum range: 0.739 1.000
- With one exception, SPI(t) > CPI

Real Data - Observations

 Cost & schedule standard deviations are comparable





- Variation greater than seen previously
- Change in index values greater than expected
 - Four projects had changes greater than 0.10 between 80 and 100 percent complete
 - Seven had changes greater than 0.05
 - Not supportive of Christensen CPI stability

• • • Forecast Result (90% Confidence)









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Project #1 Observations

• Difference between upper & lower CLs becoming smaller as percent complete increases



• CPI is very stable between 50 and 100%



- SPI(t) consistently worsens
 - IEAC(t)_H beginning at 30% complete proved to be very close to the eventual final duration

Test Result – One Scenario

TILD





$= - \frac{10\%}{10\%}$													
	**** Project Number ****												
Bounds	1	2	3	4	5	6	7	8	9	10	11	12	Probability
Cost High	Ha	Ha	Ho	Ha	Ho	Ha	Ho	Ha	Ha	Ho	Ha	Ha	0.927
	0.000	0.000	0.500	0.044	0.500	0.000	0.844	0.000	0.000	0.116	0.000	0.000	
Cost Low	Ha	Ho	Ha	Ha	Ha	На	Ha	Ha	Ha	Ha	Ha	Ha	1.000
	0.000	0.804	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	
Schedule High	Ha	Ha	Ha	Ha	Ha	Ha	Ha	Ha	Ha	Ha	Ho	Ha	1.000
	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.003	0.000	0.000	0.132	0.000	
Schedule Low	Ha	Ha	Но	Ha	Ha	Ha	Ha	Ha	Ha	Ha	Ha	Ho	0.997
	0.000	0.000	0.791	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	1.000	
									Composite Probability				1.000

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Test Result Observations

 Ha & Ho are the alternate and null hypothesis test results for each project

 The numbers beneath Ha & Ho are the computed values for the test statistic



• The probability results for both cost & schedule forecasts indicate high reliability throughout the entire period

Compiled Test Results

	Prediction Probability									
	<u>Bounds</u>		***	90% Confidence	95% Confidence	98% Confidence				
Project Management Institute College of Performance Management			\geq 10% Complete \geq 30% Complete \geq 60% Complete \geq 10% Co		≥ 10% Complete	≥ 10% Complete				
	Cost	High	0.613	0.613	0.927	0.613	0.927			
	COSI	Low	1.000	1.000	0.981	1.000	1.000			
Earned Schodula	Schedule	High	1.000	1.000	1.000	1.000	1.000			
Domedule		Low	0.997	0.981	0.997	0.997	0.997			

Compiled Test Analysis

o In general, expectation realized





- As confidence level increases, probability of obtaining Ha increases
- As data is restricted nearer to the project completion, the probability of obtaining Ha increases
- Safest forecast regardless of data set is 98% confidence level
- Trade-off: the larger the confidence, the greater the likelihood of overstating the upper and lower limits

Compiled Test Analysis

• Reliable forecasts are seen for the 90% confidence at 60% complete scenario





 Compares favorably to previous work, where it was determined that 60% complete is the generalized stability point for the CPI

 Adds credence to assertion that as index becomes more stable a lower confidence level can be applied with the expectation of obtaining reliable forecasts

Compiled Test Analysis

 Recall comparison of final values of cost and schedule indexes: SPI(t) > CPI





- Achieving schedule likely has priority
- Focus on schedule possibly caused costs to be skewed high
- The tendency toward high cost could explain generally lower probability values for IEAC_H
- Application of 90% confidence level at 10% complete conjectured to be generally reliable







- Statistical forecasting of high and low outcomes tested for reliability
 - Confidence Levels: 90%, 95%, 98%
 - Data Sets: 10%, 30%, 60%
- Generally, greater reliability the higher the confidence level and the larger the percent complete
 - Schedule forecast more reliable than for cost
- Due to unique characteristics of data tested, 90% confidence postulated to be appropriate for most circumstances

• • Final Remarks





 independent of size or type of project
 The statistical method has the potential to greatly enhance management information for the purpose of project control

• The method put forth is generally

applicable and encouraged -

 Tool for trialing available at the calculators page of the Earned Schedule website (Statistical Prediction Calculator)





Frontier," CrossTalk, June 2006: 20-23 "Prediction of Project Outcome: The Application of Statistical Methods to Earned Value Management and Earned Schedule Performance Indexes," International

• "Statistical Methods Applied to EVM: The Next

- Journal of Project Management, February 2009 (pending)
- Earned Schedule Website: www.earnedschedule.com